Computational fluid dynamic analysis of calcified coronary plaques: correlation between hemodynamic changes and cardiac image analysis based on left coronary bifurcation angle and lumen assessments

The purpose of this study was to determine the relationship between left coronary bifurcation angle and significant coronary stenosis with use of coronary CT angiography (CCTA)-generated computational fluid dynamics (CFD) analysis when compared to the CCTA analysis of coronary lumen stenosis with invasive coronary angiography (ICA) as the reference method. Eleven patients with calcified plaques at the left coronary artery tree who underwent CCTA and ICA examinations were included in the study. CFD simulation of left coronary models was performed to analyse hemodynamic changes including wall shear stress, wall pressure and flow velocity. The mean bifurcation angle was measured $83.3 \pm 17.1^{\circ}$ and $83.3 \pm 17.0^{\circ}$ on CCTA and ICA, respectively, with no significant difference (p=0.99). Of 15 significant stenosis at left anterior descending (LAD) and left circumflex (LCx) on CCTA, only 3 of them were confirmed to be > 50% stenosis on ICA. Wall shear stress was noted to increase in the LAD and LCx models with significant stenosis and wider angulation ($> 80^{\circ}$), but remained no change in most of the other coronary models with no significant stenosis and narrower angulation. Wall pressured was decreased at the significant stenotic lesions, while flow velocity was increased with flow turbulence at the post-stenotic sites. This study further clarifies the direct correlation between left coronary bifurcation angle and significant stenosis, with angulation measurement being more accurate than lumen assessment for diagnosing significant stenosis.

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Coronary CT angiography (CCTA) is a widely performed imaging modality for the diagnostic assessment of coronary artery disease. Rapid developments in multi-slice CT scanning techniques enable accurate analysis and characterization of coronary plaque by CCTA [1-3]. The main factor that limits diagnostic performance of CCTA is due to blooming artifact which arises from severe calcification in the coronary artery. This results in high false positive rate, thus, compromising the specificity and positive Zhonghua Sun¹*, and Thanapong Chaichana² ¹Department of Medical Radiation Sciences, Curtin University, Perth, Western Australia, 6845, Australia ²Biomechanical Electronics Research Group, Department of Mathematics and Computer Science, Liverpool Hope University, Hope Park, Liverpool, England, United Kingdom *Author for correspondence: Tel.: +6189266 7509 Fax: +61892662377 z.sun@curtin.edu.au

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predictive value of CCTA to a greater extent. It has been reported that in the presence of highly calcified plaques, the specificity of CCTA ranges from 18% to 53% based on degree of coronary lumen stenosis [4-8]. To overcome this limitation, strategies have been proposed to improve the specificity including application of image post-processing algorithms to minimize the artifact effect or use of high spatial resolution to improve lumen assessment [9-11]. Using left coronary bifurcation angle to determine significant coronary stenosis is another approach for diagnosis of calcified coronary plaques with promising results reported when compared to the conventional method of coronary lumen assessment [5,12,13].

The rationale of taking into account coronary bifurcation angle for assessment of coronary artery disease is due to the well-known fact that there is close association between hemodynamic changes and atherosclerosis development at bifurcation regions [14-17]. Plaque proliferation occurs when wall shear stress is decreased due to increased bifurcation angle or in the vascular areas of abrupt curvatures [14,18]. Wider bifurcation angles have been shown to be associated with higher-risk plaques in comparison with the arteries with narrower angles, highlighting the correlation between bifurcation angle and plaque development [14,19]. Despite these studies assessing the bifurcation angle and hemodynamic changes in relation to coronary artery disease or plaque development, to the best of our knowledge, no report is available on the investigation of relationship between bifurcation angle and coronary lumen assessment and corresponding hemodynamics. Thus, the purpose of this study is to further confirm the diagnostic value of using bifurcation angle for assessment of calcified coronary plaques by correlating hemodynamic changes to the coronary artery with degree of coronary stenosis based on CCTA. 3D reconstruction of coronary artery and plaques with numerical simulation using computational fluid dynamics (CFD) based on patient-specific imaging data has been increasingly used in recent years to study hemodynamics in cardiovascular disease [20-22]. We hypothesized that the method of using bifurcation angle with CCTA is closely related to the corresponding hemodynamic changes with CCTA-derived CFD analysis in the diagnosis of calcified plaques.

Materials and Methods

Study population

Patients undergoing CCTA and invasive coronary angiography (ICA) for the diagnosis of coronary artery disease were retrospectively reviewed. Only those patients with calcified plaques in the left coronary artery tree detected by CCTA with degree of coronary stenosis confirmed by ICA were included in the study. Out of 40 patients with CCTA and ICA imaging examinations, 11 (7 males, mean age: 62.2 ± 6.8 years) were selected for this study, while the remaining patients were excluded due to presence of non-calcified or mixed plaques (n = 20), coronary stents (n = 5), and poor image quality (n = 4).

All patients were scanned with the second-generation of dual-source CT (Somatom Definition Flash, Siemens Healthcare, Forchheim, Germany). The scanning parameters, contrast injection and patient preparation in terms of heart rate control for CCTA protocol and ICA procedure were described previously [5].

All procedures performed in this study were in accordance with the ethical standards of the institutional and/or national research committee. Ethics approval was waived in this study as data acquisition of CCTA comprises routine diagnostic examination of coronary artery disease. Due to the retrospective nature of this study, informed consent was not required from the patients.

Measurement of left coronary bifurcation angle

Left coronary bifurcation between left anterior descending (LAD) and left circumflex (LCx) was measured on both CCTA and ICA images. Measurements were performed by two investigators (with 8 and more years of experience in cardiac CT imaging) with angle measured during diastolic phases during CCTA and ICA images with the aim of obtaining maximum angulation during this cardiac phase. Three consecutive angle measurements were obtained with the mean value taken as final to avoid intra- and inter-observer disagreement. A degree of > 80° bifurcation angle is used as a cut-off value to determine significant coronary artery disease or stenosis, according to previous studies [13,19,23-25].

Generation of left coronary artery model for CFD analysis

Segmentation of CCTA volume data was performed with a semiautomatic technique to remove bony and other structures while only extracting the topology of the left coronary artery tree consisting of left main stem, LAD and LCx branches, identifying coronary plaques and segmenting lumen boundary along the left coronary tree. Details of image post-processing and segmentation have been described in previous studies [26,27]. In brief, 3D volume datasets were post-processed on a workstation with Analyze 12.0 (Analyze Direct, Inc., Lexana, KS, USA). Image post-processing and segmentation was based on CT number thresholding technique, with scan-related artifacts and soft tissues being removed in 2D axial and 3D reconstructed images. The purpose of image Computational fluid dynamic analysis of calcified coronary plaques: correlation between hemodynamic changes and cardiac image analysis based on left coronary bifurcation angle and lumen assessments

segmentation was to generate 3D surface models which consist of left main stem coronary artery, LAD and LCx and its main side branches. The 3D left coronary artery surface models of these cases were saved in "binary STL (stereo-lithography) format" for generation of computational models.

The binary STL files were transferred to a workstation for reconstruction purposes and CFD simulation. Although the original rough surface geometry of left coronary artery was kept, the surface models were smoothed to remove some artifacts (such as non-physical artifacts caused by sharp edges). The computational left coronary artery models were saved into "STL format" for generation of computational elements of the models using ANSYS ICEM CFD version 12v (ANSYS, Inc., Canonsburg, PA, USA). CFD simulations were conducted with implementation of parameters of realistic physiological boundary conditions in these models, and this has been described in detail in previous studies [14,26,28]. In brief, a time dependent simulation was computed, with the hemodynamic profiles including flow velocity, wall pressure and wall shear stress (WSS) being calculated and compared with findings from image analysis by CCTA and ICA in terms of the bifurcation angle and lumen stenosis.

Generation of medical computing for CFD modelling

The essential parameters of CFD modelling were mainly chosen to conduct medical image computing for cardiovascular blood flow analysis. The transient flow replicating both systolic and diastolic phases was applied as the boundary flow computation of an inflow condition [14,26]. The parameters of rheological properties were applied as the blood flow was hypothesized to be laminar flow in the small region of blood vessels, the viscosity of the blood was assumed to be 0.0035 Pas, and density of the blood was premised to be 1060 kg/m³. Blood modelling was assumed to be an incompressible fluid and a Newtonian fluid model. Blood vessel wall modelling was genuinely defined as no-slip condition which was exerted at the walls, and a rigid wall model was assumed to be on a micro millimeter of vascular movement of small vessels. The ANSYS CFX version 12 (ANSYS, Inc.) was used to solve the govern simulation equation as of Navier Stokes equation. Hemodynamic visualisations were analysed during the systolic and diastolic phases for statistical analysis and the presented hemodynamic factors in terms of WSS, wall pressure and flow velocity were chosen effectively to reflect actual effect upon the purpose of the study.

Table 1: Correlation of CFD simulations with coronary CT angiography and invasive angiography findings.										
No. of Cases	Bifurcation angle on CCTA (°)	Bifurcation angle on ICA (°)	Degree of lumen stenosis on CCTA		Degree of lumen stenosis on ICA					Risk Assessment
			LAD	LCx	LAD	LCx	WSS	Wall pressure	Flow velocity	Angulation/ Lumen
1	99	99.5	74%	33%	89%	25%	High at LAD stenotic site	Decreased at LAD stenotic site	Increased at LAD stenotic site	A
2	78	70	62%	-	44%	-	No significant change	Slightly decreased at LAD	Slightly turbulent at LAD	~
3	53	55.7	80%	65%	42%	48%	No significant change	No significant change	Laminar flow	\checkmark
4	105	105	72%	87%	44%	77%	Increased at LAD and LCx	Decreased at LCx stenotic site	High at LCx stenotic site	▼
5	68.5	75	72%	-	25%	-	No significant change	No significant change	Laminar flow	\checkmark
6	91.8	90	69%	-	29%	-	No significant change	No significant change	Laminar flow	✓
7	108	115	60%	26%	15%	2%	Increase at LAD	No significant change	High at LAD	▼
8	76.2	77	88%	68%	28%	45%	Slightly increased at LM	No significant change	Slight increased at LM and LAD	▼
9	91.5	85	61%	49%	61%	5%	High at LAD stenotic site	No significant change	Slight increased at LAD	
10	74	78	57%	71%	39%	48%	No significant change	No significant change	Laminar flow	\checkmark
11	71.3	70.7	51%	-	19%	-	High at LM	No significant change	Slightly increased at LM	▼

CCTA-coronary CT angiography, ICA-invasive coronary angiography, LM-left main stem, LAD-left anterior descending, LCx-left circumflex, WSS-wall shear stress, ▲ high risk of coronary stenosis and angulation, ▼ low risk of coronary stenosis and angulation, ✓ normal coronary lumen with no risk of developing significant stenosis.

Statistical analysis

Data were entered into SPSS 24.0 for statistical analysis (SPSS Inc, Chicago., IL, USA). Continuous variables were expressed as mean \pm standard deviation, while categorical variables were presented as percentages. Chi-square test was used for analysis of categorical variables or Fisher's Exact test. One sample T test was used to determine the differences of bifurcation angle between CCTA and ICA. A p value of < 0.05 was considered statistically significant.

Results

Table 1 shows the distribution of coronary plaques in the left coronary arteries with corresponding bifurcation angle, coronary lumen measurements on CCTA and ICA, as well as the CFD analysis in each case. The mean bifurcation angle measured with CCTA and ICA was $83.3 \pm 17.1^{\circ}$ and $83.3 \pm 17.0^{\circ}$ respectively, with no significant difference between these two modalities (p = 0.99). However, coronary stenosis was overestimated in 80% of the lumen assessment on CCTA, as shown in the table. Significant stenosis (> 50%) was observed at LAD by CCTA in all of the 11 cases, while only two of them were confirmed to be > 50% stenosis by ICA. Similarly, of four LCx stenosis of > 50% on CCTA, only one was confirmed to be significant by ICA. Figures 1A and 1B are an example of calcified plaques at LAD with overestimated stenosis on CCTA, but ICA shows mild stenosis.

Table 1 also shows the CFD analysis of these patients with findings directly correlated with the bifurcation angle measurement, but not with the degree of lumen stenosis. WSS was noted to increase in the LAD and LCx models with significant stenosis and wider angulation (>80°), but remained no change in most of the coronary models with no significant stenosis or narrower angulation. WSS was slightly increased at the left main (LM) stem regions in

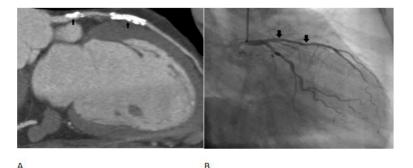


Figure 1: Severe calcification in the coronary artery results in overestimation of coronary lumen stenosis. A: Curved planar reformatted coronary CT angiography (CCTA) shows extensively calcified plaques (arrows) at the proximal segment of left anterior descending (LAD) with more than 80% lumen stenosis. **B:** Invasive coronary angiography only shows mild stenosis of <50% (arrows), indicating the overestimation of degree of stenosis in CCTA.

two cases, although there was no significant lumen stenosis on ICA. Wall pressure was decreased in two of the three models with significant coronary stenosis, while flow velocity was increased with post-stenotic flow turbulence in the presence of significant stenosis at the LAD and LCx. Figures 2A-2C shows CFD modelling of a patient with wide bifurcation angle and significant lumen stenosis at LAD, while Figures 3A-3C is another example of a narrow bifurcation angle without significant stenosis.

Discussion

This study is conducted to further clarify the diagnostic value of using bifurcation angle for determination of coronary artery stenosis with use of CFD modelling when compared to the conventional approach of using coronary lumen stenosis. Results showed that there is a direct correlation between left coronary bifurcation angle and corresponding hemodynamic changes with wider angulation and significant stenosis associated with increased WSS and flow velocity and decreased all pressure changes. In contrast, the narrower angulation without significant stenosis led to no changes to the hemodynamic parameters on CFD analysis. Therefore, this study further strengthens the idea that bifurcation angle is more accurate than coronary lumen stenosis for diagnostic assessment of calcified coronary plaques.

The role of wall shear stress on atherosclerosis has been widely studied with low shear stress contributing to plaque formation, while high shear stress leading to plaque rupture [22]. Simulation of coronary flow conditions in a patient-specific coronary model is available with use of CCTA-generated CFD models. Hemodynamic analysis using CFD is considered to be more accurate than CCTA-based lumen analysis for determining significant coronary stenosis. This has been confirmed by several multicentre studies comparing CCTA-generated CFD with CCTA. The DISCOVER-FLOW, DeFACTO and NXT trials are three representative studies showing that CCTAderived fractional flow reserve (FFRCT) is superior to CCTA with improved diagnostic value for diagnosis of ischemic coronary lesions on both per-patient and per-vessel analysis [29-31]. This has significant health and economic implications due to the beneficial effects of using FFRCT as a reliable gatekeeper to invasive procedures and revascularization. These studies also support the use of CFD technique for detection of significant coronary stenosis because the degree of coronary lumen stenosis is not a reliable indicator to determine functional significant of the lesion.

CCTA-generated CFD analysis of coronary hemodynamics has gained increasing attention recently.

Research article

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Park et al. in their recent study analysed hemodynamic changes in 80 patients with plaques located at the left coronary artery tree [20]. Higher WSS was found to be at stenotic coronary segments when compared with nonstenotic segments, with WSS providing more valuable information than lumen narrowing in determining adverse plaque characteristics and differentiating highrisk plaques. The study suggests that patient-specific CFD modelling based on CCTA provides insight into elucidating the correlation between hemodynamic changes and plaque features and associated clinical events, thus, improving risk stratification for patients with coronary artery disease. This is consistent with other studies highlighting the association between high WSS and plaque progression and plaque vulnerability [32,33]. However, the main limitation of these studies is lack of looking at the calcified plaque with regard to the left coronary bifurcation angle and corresponding CFD analysis.

This study was designed to fill this gap by looking at the left coronary bifurcation angle in relation to the hemodynamic changes as assessed by CCTA-based CFD analysis. Findings are consistent with previous reports indicating less favourable WSS distributions for wider angulated coronary arteries [14,15,34], as well as supporting the previous report of direct correlation between bifurcation angle and intraluminal changes of coronary plaques [35]. However, Beier et al. in their study did not notice significant effect of angulation on the flow dynamic changes to the left coronary artery. Their analysis was based on idealized and patientspecific left coronary artery with different angulations. Their results showed that vessel shape features including tortuosity, diameter or incoming angle produce more impact than bifurcation angle on WSS distribution [36]. Further research is required to clarify the correlation between bifurcation angle and WSS changes in the left coronary artery.

This study has some limitations. First, the sample size is small, despite correlating CCTA findings with ICA which is regarded as the gold standard for lumen assessment. Further, significant stenosis was only confirmed in 3 out of 15 coronary lesions. Studies with inclusion of more patients with significant stenosis and different angulations are needed to verify our results. Second, CFD simulation was conducted under rest condition of cardiac physiology. To represent realistic situation of cardiac cycle, CFD simulation under hyperemia should also be conducted. Finally, we did not analyse plaque characteristics to identify vulnerable plaques as we only included calcified plaques in the

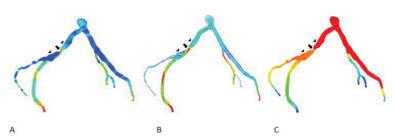


Figure 2: Association between wider angulation and hemodynamic changes by computational fluid dynamics (CFD). Left coronary bifurcation angle between left anterior descending and left circumflex (LCx) was measured 105° with significant stenosis at LCx on CCTA and ICA in a 58-year-old man. Wall shear stress and flow velocity were increased at the stenotic site of LCx (A and B), while wall pressure was decreased at the same location (C). Arrow refers to the stenotic region at LCx, while arrowheads point to the pre- and post-stenotic locations.

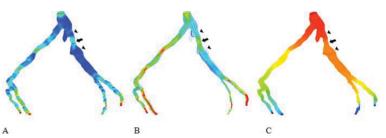


Figure 3: Association between narrower angulation and hemodynamic changes by CFD. Left coronary bifurcation angle between left anterior descending (LAD) and left circumflex (LCx) was measured 53° and 55.7° on CCTA and ICA in a 65-year-old male, respectively. Significant stenosis (>60%) was noticed at LAD and LCx on CCTA, but no significant stenosis (42-48%) was confirmed on ICA. There was no significant change to the hemodynamic parameters including wall shear stress, flow velocity and wall pressure (A-C). Arrow refers to the mild stenotic site of LAD, while arrowheads point to the pre- and post-stenotic locations.

left coronary artery tree, since severe calcification is associated with overestimation of coronary lumen stenosis, thus, leading to high false positive rate. Further studies with a focus on plaque features in addition to the bifurcation angle measurement are needed to determine the relationship between angulation and development of high-risk plaques.

Conclusion

In conclusion, this study shows a direct correlation between wider left coronary bifurcation angle and corresponding hemodynamic changes, mainly the wall shear stress as assessed by CCTA-generated CFD analysis. Results further confirm that coronary bifurcation angle is more accurate than lumen assessment for diagnosing significant stenosis in the presence of calcified plaques. Incorporation of CFD findings into CCTA analysis will add clinical value for differentiating significant stenosis or high-risk plaques in patients with suspected coronary artery disease. Further research on a large cohort with analysis of plaque characteristics is warranted.

Executive summary

- The purpose of this study was to determine the relationship between left coronary bifurcation angle and significant coronary stenosis with use of coronary CT angiography (CCTA)-generated computational fluid dynamics (CFD) analysis when compared to the CCTA analysis of coronary lumen stenosis with invasive coronary angiography (ICA) as the reference method.
- This study further clarifies the direct correlation between left coronary bifurcation angle and significant stenosis, with angulation measurement being more accurate than lumen assessment for diagnosing significant stenosis.

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